

KUMAUN UNIVERSITY NAINITAL

DRAFT

National Education Policy-2020

**Common Minimum Syllabus for Uttarakhand State
Universities and Colleges**

**Four Year Undergraduate Programme
FYUP/Honours Programme/Master in Science**

MATHEMATICS SYLLABUS

DEPARTMENT OF MATHEMATICS

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List of Papers (DSC, DSE, GE) with Semester Wise Titles for ‘Mathematics’

Year	Semester	Course	Paper Title	Credits	
Certificate in Science (Mathematics as one of the major Subject)					
FIRST YEAR	I	DSC Maths1	Fundamental Mathematics-I	Theory	4
	II	DSC Maths2	Fundamental Mathematics-II	Theory	4
Diploma in Science (Mathematics as one of the major Subject)					
SECOND YEAR	III	DSC Maths3	Differential Calculus	Theory	4
		DSE Maths1	Geometry	Theory	4
	IV	DSC Maths4	Integral Calculus	Theory	4
		DSE Maths2	Group Theory	Theory	4
Bachelor of Science (Mathematics as one of the major Subject)					
THIRD YEAR	V	DSC Maths5	Analysis	Theory	4
		DSE Maths3	Ring Theory	Theory	4
	VI	DSC Maths6	Linear Algebra	Theory	4
		DSE Maths4	Differential Equations	Theory	4
Bachelor of Science (Honors)					
FOURTH YEAR	VII	DSC Maths7	Real Analysis	Theory	4
		DSE Maths5	Topology	Theory	4
		DSE Maths6	Differential Geometry	Theory	4
		DSE Maths7	Dynamics of Rigid Bodies	Theory	4
	VIII	DSC Maths8	Complex Analysis	Theory	4

		DSE Maths8	Algebra	Theory	4
		DSE Maths9	Partial Differential Equations	Theory	4
		DSE Maths10	Tensor Calculus	Theory	4
Master of Science (Mathematics)					
FIFTH YEAR	IX	DSC Maths9	Linear Algebra	Theory	4
		DSE Maths11	Measure Theory	Theory	4
		DSE Maths12	**Mathematical Statistics / Number Theory	Theory	4
		DSE Maths13	**Fluid Dynamics / Discrete Mathematics	Theory	4
	X	DSC Maths10	Functional Analysis	Theory	4
		DSE Maths14	Numerical Methods	Theory	4
		DSE Maths15	**Operations Research / Relativity	Theory	4
		DSE Maths16	**Special Functions / Riemannian Geometry / Introduction to programming using MATLAB	Theory	4

** A Candidate is required to opt any one specialization out of the available specializations in fifth Year.

Abbreviations-

DSC-Discipline Specific Course; DSE- Discipline Specific Electives; GE-Generic Electives;

Program Outcomes (POs) (Undergraduate Programme) :

After this programme:

PO 1.	Students will have a firm foundation in the fundamentals and applications of mathematics and scientific theories.
PO 2.	Students will develop skills in problem solving, critical thinking and analytical reasoning as applied to scientific problems.
PO 3.	Students will be able to explore new directions to pursue higher studies in science subjects.
PO 4.	Students will be able to contest and qualify different competitive exams where graduation degree is one of the essential qualifications.
PO 5.	Students will be able to function as a member of an interdisciplinary problem-solving team.

Program Outcomes (POs) (Honors Programme):

After this programme:

PO 6.	
PO 7.	
PO 8.	

Program Outcomes (POs) (Master Degree Programme):

After this programme:

PO 9.	
PO 10.	
PO 11.	
PO 12.	

PROGRAM SPECIFIC OUTCOMES (PSOS)

First Year	Certificate in Science (Mathematics as one of the major Subject)
	Certificate in Science will give students a basic knowledge of mathematics. Two other major subjects needed for the study of other courses in forthcoming years. It will enable students to join the diploma course (semester III and IV) in any University or College of Higher education in Uttarakhand
Second Year	Diploma in Science (Mathematics as one of the major Subject)
	Diploma will enable students to join the Bachelor of Science course (semester V and VI) in any University or College of Higher education in Uttarakhand
Third Year	Bachelor of Science (Mathematics as one of the major Subject)
	Upon completion of a degree, students will be eligible for Master Degree in any of the major subject in any of the higher institutions of India. It will give students an ability of critical thinking and scientific study of any discipline. Students after getting Bachelor

	degree will be eligible for all the competitive examinations where graduation is an essential qualification.
Fourth Year	<p>Bachelor of Science (Honors)</p> <p>After completing the degree of Bachelor of science (Honors), students will be eligible for one year Master degree programme in the subject. It will explore students to advanced topics / techniques used in mathematics and also will help them to develop the ability to formulate real life problems mathematically and solve using these techniques. They will be eligible to pursue their career in various fields of academics, research and industry as well as to obtain master degree in Mathematics.</p>
Fifth Year	<p>Master of Science (Mathematics)</p> <p>The Master of Science in Mathematics Programme will enable students to join Ph. D. program in universities and research institutes within India or abroad. The student would get research experience by doing research projects in the last semester under the supervision of faculty which will make them eligible to open up several career options in mathematics and other branches of mathematical sciences and physical sciences.</p>

Department of Mathematics

Semester-I

Certificate in Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC COURSE (DSC Maths1)- Fundamental Mathematics-I

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths1: Fundamental Mathematics-I	4	3	2	0	Passed Class XII with Mathematics	Nil

Certificate in Science (Mathematics as one of the major Subject)

Programme :	<i>Certificate in Science (Mathematics as one of the major Subject)</i>	Year: I	Semester: I Paper: DSC Maths1
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Subject: Mathematics

Course: DSC Maths1	Course Title: Fundamental Mathematics-I
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Course Outcomes: This paper is a fundamental course for intermediate pass students who are going to study mathematics as one of the major subjects for their graduation degree. It gives basic knowledge and background to understand other courses either in mathematics or physics.

Credits: 4		Discipline Specific Course
Max. Marks: As per Univ. rules		Min. Passing Marks: As per Univ. rules
Unit	Content	Number of Hours
Unit I	Theory of Equations: Relations between Roots and Coefficients of algebraic equations, Transformation of equations, Descartes rule of signs, Solutions of Cubic and Bi-quadratic equations.	10-15
Unit II	Matrices: Basic concepts of matrices, Types of matrices, Transpose, trace and determinant of a matrix, Elementary operations, Row Reduced echelon form, Rank and inverse of a matrix, Normal form of a matrix, Solutions of a system of linear equations, Characteristic equation of a	12-15

	matrix, eigenvalues, eigenvectors, Cayley-Hamilton theorem.	
Unit III	Trigonometry: Complex numbers with elementary properties, De-Moivre's theorem, Exponential Functions, Euler's theorem, Circular and hyperbolic functions of complex variables together with their inverses, Logarithmic Functions, Gregory's series, Summation of Trigonometric series.	10-15
Unit IV	Vector Calculus: Dot product, cross product and their geometric interpretation, Triple products, Reciprocal vectors, Ordinary differentiation of vectors, Differential operators-Del, Gradient, Divergence and Curl, Line, surface and volume integrals, Simple applications of Gauss divergence theorem, Green's theorem and Stokes' theorem.	12-15

Books Recommended:

C. C. MacDuffee: *Theory of Equations*, John Wiley & Sons, 1954.

Shanti Narayan and P. K. Mittal: *A Text Book of Vector Calculus*, S. Chand & Company, 1987.

J. G. Chakravorty and P. R. Ghosh: *Analytical Geometry and Vector Analysis*, U. N. Dhur & Sons Pvt. Ltd, 1973.

Murray Spiegel, Seymour Lipschutz and Dennis Spellman: *Vector Analysis*, Schaum's Outline Series, McGraw Hill Edition, 2017.

R. K. Sharma, S. K. Shah and A. G. Shankar: *Complex Numbers and the Theory of Equations*, Anthem Press, 2011.

N. Saran and S. N. Nigam: *Introduction to vector analysis*, Pothishala publication, Allahabad, 1990.

Further Readings:

William Snow Burnside and Arthur William Panton: *The Theory of Equations Vol. I*, Nabu Press, 2011.

Leonard E. Dickson: *First Course in the Theory of Equations*, Merchant Books, 2009.

Fuzhen Zhang: *Matrix Theory- Basic Results and Techniques*, Springer, 1999.

K. B. Dutta: *Matrix and Linear Algebra*, Prentice Hall of India, 2004.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-II

Certificate in Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC COURSE (DSC Maths2)- Fundamental Mathematics -II

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths2: Fundamental Mathematics-II	4	3	2	0	Passed Class XII with Mathematics	Nil

Certificate in Science (Mathematics as one of the major Subject)

Programme : <i>Certificate in Science (Mathematics as one of the major Subject)</i>	Year: I	Semester: II Paper: DSC Maths2
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Subject: Mathematics

Course: DSC Maths2	Course Title: Fundamental Mathematics-II
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Course Outcomes: This paper is a fundamental course for intermediate pass students who are going to study mathematics as one of the major subjects for their graduation degree. It gives basic knowledge and background to understand other courses either in mathematics or physics.

Credits: 4	Discipline Specific Course
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
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Unit I	Preliminaries: Sets, Operations on sets, Index set and family of sets, Relations, Equivalence relations and partitions, Functions, Composition of functions, Infinite sets and cardinality, Cantor set, Principle of mathematical induction.	10-15
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Unit II	Numerical Sequence and Series: Sequences, theorems on limit of sequences, Infinite series, series of non-negative terms, Various tests for convergence, Alternating series, Leibnitz's theorem, Absolute convergence, Conditional convergence.	12-15
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Unit III	Partial Derivatives: Functions of more than one variable, Partial Derivatives, Euler's Theorem for Homogeneous Functions, Jacobians and their applications, Chain rule.	12-15
Unit IV	Polar Geometry: Polar coordinate system, Polar equation of a conic, Chords, Tangent and Normal to a conic, Tracing of conics.	10-15

Books Recommended:

C. C. MacDuffee: *Theory of Equations*, John Wiley & Sons, 1954.

Shanti Narayan and P. K. Mittal: *A Text Book of Vector Calculus*, S. Chand & Company, 1987.

J. G. Chakravorty and P. R. Ghosh: *Analytical Geometry and Vector Analysis*, U. N. Dhur & Sons Pvt. Ltd, 1973.

Murray Spiegel, Seymour Lipschutz and Dennis Spellman: *Vector Analysis*, Schaum's Outline Series, McGraw Hill Edition, 2017.

R. K. Sharma, S. K. Shah and A. G. Shankar: *Complex Numbers and the Theory of Equations*, Anthem Press, 2011.

N. Saran and S. N. Nigam: *Introduction to vector analysis*, Pothishala publication, Allahabad, 1990.

Further Readings:

William Snow Burnside and Arthur William Panton: *The Theory of Equations Vol. I*, Nabu Press, 2011.

Leonard E. Dickson: *First Course in the Theory of Equations*, Merchant Books, 2009.

Fuzhen Zhang: *Matrix Theory- Basic Results and Techniques*, Springer, 1999.

K. B. Dutta: *Matrix and Linear Algebra*, Prentice Hall of India, 2004.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-III

Diploma in Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC COURSE (DSC Maths3)- Differential Calculus

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths3: Differential Calculus	4	3	2	0	Passed Class XII with Mathematics	Completed DSC Maths1 and DSC Maths2

Diploma in Science (Mathematics as one of the major Subject)

Programme :	<i>Diploma in Science (Mathematics as one of the major Subject)</i>	Year: II	Semester: III Paper: DSC Maths3
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Subject: Mathematics

Course: DSC Maths3 **Course Title:** Differential Calculus

Course Outcomes: This paper provides detailed knowledge of differentiation and integration of various classes of functions. It relates and gives an analytical aptitude for various mathematical problems. After completing this course students will be able to understand basic concepts of calculus and able to apply these concepts in other areas of study especially physics and engineering.

Credits: 4	Discipline Specific Course	
Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules	
Unit	Content	Number of Hours
Unit I	Limit, Continuity and Differentiability: Functions of one variable, Limit and Continuity of a function, Properties of continuous functions, Classification of Discontinuities, Differentiability of a function, Rolle's Theorem, Mean value theorems and their geometrical interpretations, Applications of mean value theorems. Successive Differentiation, n^{th} Differential coefficient of functions, Leibnitz Theorem; Taylor's Theorem, Maclaurin's	10-15

	Theorem, Taylor's and Maclaurin's series expansions, Indeterminate forms.	
Unit II	Tangents and Normals: Geometrical meaning of dy/dx , Definition and equation of Tangent and Normal, Tangent at origin, Angle of intersection of two curves, Subtangent and Subnormal, Tangents and Normals of polar curves, Angle between radius vector and tangent, Perpendicular from pole to tangent, Pedal equation of curve, Polar subtangent and polar subnormal, Intrinsic equations.	12-15
Unit III	Curvature and Asymptotes: Curvature, Radius of curvature; Cartesian, Polar and pedal formula for radius of curvature, Tangential polar form, Centre of curvature, Asymptotes of algebraic curves, Methods of finding asymptotes, Parallel asymptotes.	12-15
Unit IV	Singular Points and Curve Tracing: Existence and classification of singular points, points of inflexion, Double Points, Cusp, Node and conjugate points, Curve tracing.	10-15

Books Recommended:

T. M. Apostol: *Calculus Vol. I*, John Wiley & Sons, 1999.

Gorakh Prasad: *Differential Calculus*, Pothishala publication, Allahabad, 2016.

M. Ray, H. S. Sharma and S. S. Seth: *Differential Calculus*, Shiva Lal Agarwal & Company, Agra.

Further Readings:

S. Lang: *A First Course in Calculus*, Springer-Verlag New York Inc., 1986.

H. Anton, I. Birens and S. Davis: *Calculus*, John Wiley & Sons, 2007.

G. B. Thomas and R. L. Finney: *Calculus*, Pearson Education, 2010.

S. Balachandra Rao and C. K. Shantha: *Differential Calculus*, New Age Publication, 1992.

Frank Ayres and Elliott Mendelson: *Calculus*, Schaum's Outline Series, McGraw Hill Edition, 2009.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-III

Diploma in Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths1)- Geometry

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths 1: Geometry	4	3	2	0	Passed Class XII with Mathematics	Nil

Certificate in Science (Mathematics as one of the major Subject)

Programme :	<i>Certificate in Science (Mathematics as one of the major Subject)</i>	Year: II	Semester: III Paper: DSE Maths1
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Subject: Mathematics

Course: DSE Maths 3 **Course Title:** Geometry

Course Outcomes: This course will enhance the understanding of mathematical concepts with geometrical/graphical interpretations. After studying this course students will be able to visualize mathematical concepts geometrically.

Credits: 4 Discipline Specific Elective

Max. Marks: As per Univ. rules Min. Passing Marks: As per Univ. rules

Unit	Content	Number of Hours
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Unit I	Direction Cosines and the Plane: Cartesian co-ordinates in 3D, Direction cosines, direction ratios and their properties, Equation of a Plane in various forms, Two sides of a plane, Length of perpendicular from a point to a plane, Angle between two planes, System of planes, Transformation of coordinates.	10-15
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Unit II	Straight Lines and the Sphere: Equation of a line in different forms, Angle between a line and a plane, Co-planar lines, Shortest distance, Length of perpendicular from a point to a line, Intersection of three planes	12-15
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	Definition and equation of a sphere, Plane section of a sphere, Intersection of two spheres, Sphere through a given circle, Intersection of a sphere and a line, Power of a point, Tangent plane, Plane of contact, Polar plane and polar lines, Pole of a plane, Conjugate points and conjugate planes, Angle of Intersection of two spheres. Radical axis and centre.	
Unit III	Cone and Cylinder: Definition and equation of a cone with various properties, Three mutually perpendicular generators, Intersection of a line with a cone, Tangent line and tangent plane, Reciprocal cone, Right circular cone, Definition and equation of a cylinder, Right circular cylinder, Enveloping cylinder, General equation of second degree.	12-15
Unit IV	The Conicoids: Central conicoids, Tangent plane, Director sphere, Normal, Plane of contact, Polar plane, Conjugate points, conjugate planes and conjugate lines, enveloping cone, Paraboloids, Plane sections of conicoids.	10-15

Books Recommended:

S.L. Loney: *The Elements of Coordinate Geometry*, McMillan and Company, London, 2018.

Shanti Narayan and P. K. Mittal: *Analytical Solid Geometry*, S. Chand & company, 2007.

P. K. Jain: *A Textbook of Analytical Geometry*, New Age Publication, 2014.

Jyoti Das: *Analytical Geometry*, Academic Publisher, 2011.

J. G. Chakravorty and P. R. Ghosh: *Analytical Geometry and Vector Analysis*, U. N. Dhur & Sons Pvt. Ltd, 1973.

Further Readings:

Henry B. Fine and H. D. Thompson: *Coordinate Geometry*, The Macmillan company, 1909.

George B. Thomas and Ross L. Finney: *Calculus and Analytic Geometry*, Pearson Education, 2010.

Robert J. T. Bell: *An Elementary Treatise on Coordinate Geometry of three dimensions*, Macmillan India Ltd., 1923.

P. R. Vittal: *Analytical Geometry-2D & 3D*, Pearson Education, 2013.

Manicavachagom T.K. Pillay: *A Textbook of Analytical Geometry (Part:1 & 2)*, Viswanathan, S., Printers & Publishers Pvt Ltd, 2009.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-IV

Diploma in Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC COURSE (DSC Maths4)- Integral Calculus

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths4: Integral Calculus	4	3	2	0	Passed Class XII with Mathematics	Completed DSC Maths2 and DSC Maths3

Diploma in Science (Mathematics as one of the major Subject)

Programme :	<i>Diploma in Science (Mathematics as one of the major Subject)</i>	Year: II	Semester: IV Paper: DSC Maths4
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Subject: Mathematics

Course: DSC Maths4 **Course Title:** Integral Calculus

Course Outcomes: This paper provides detailed knowledge of differentiation and integration of various classes of functions. It relates and gives an analytical aptitude for various mathematical problems. After completing this course students will be able to understand basic concepts of calculus and able to apply these concepts in other areas of study especially physics and engineering.

Credits: 4		Discipline Specific Course
Max. Marks: As per Univ. rules		Min. Passing Marks: As per Univ. rules
Unit	Content	Number of Hours
Unit I	Definite Integrals: Integral as a limit of sum, Properties of Definite integrals, Summation of series by integration, Differentiation and integration under the integral sign.	10-15
Unit II	Beta and Gamma function: Beta function, Gamma function, Recurrence formula and other relations, Relation between Beta and Gamma function, Evaluation of integrals using Beta and Gamma functions.	12-15

Unit III	Multiple Integrals: Double integrals, Repeated integrals, Evaluation of Double integrals, Double integral in polar coordinates, Change of order of integration in Double integrals, Triple integrals, Evaluation of Triple integrals, Dirichlet's theorem and its Liouville's extension.	12-15
Unit IV	Geometrical Applications of Definite Integrals: Area bounded by curves (quadrature), Rectification (length of curves), Volumes and Surfaces of Solids of revolution.	10-15

Books Recommended:

T. M. Apostol: *Calculus Vol. I*, John Willey & Sons, 1999.

M. Ray, H. S. Sharma and S. S. Seth: *Differential Calculus*, Shiva Lal Agarwal & Company, Agra.

M. Ray, H. S. Sharma and S. S. Seth: *Integral Calculus*, Shiva Lal Agarwal & Company, Agra.

Further Readings:

S. Lang: *A First Course in Calculus*, Springer-Verlag New York Inc., 1986.

H. Anton, I. Birens and S. Davis: *Calculus*, John Wiley & Sons, 2007.

G. B. Thomas and R. L. Finney: *Calculus*, Pearson Education, 2010.

S. Balachandra Rao and C. K. Shantha: *Differential Calculus*, New Age Publication, 1992.

Frank Ayres and Elliott Mendelson: *Calculus*, Schaum's Outline Series, McGraw Hill Edition, 2009.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-IV

Diploma in Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths2)- Group Theory

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths2: Group Theory	4	3	2	0	Passed Class XII with Mathematics	Completed DSC Maths1 and DSC Maths2

Diploma in Science (Mathematics as one of the major Subject)

Programme : *Diploma in Science (Mathematics as one of the major Subject)* Year: II Semester: III
Paper: DSE Maths2

Subject: Mathematics

Course: DSE Maths2 Course Title: Group Theory

Course Outcomes: This course is useful to understand the concepts of algebraic structures and their properties. It will help the students for better understanding of other subjects, especially atomic structures in chemistry and certain concepts of physics.

Credits: 4 Discipline Specific Elective

Max. Marks: As per Univ. rules Min. Passing Marks: As per Univ. rules

Unit	Content	Number of Hours
Unit I	Groups: Binary operation and Algebraic structure, Abelian groups, Noncommutative groups and Subgroups.	10-15
Unit II	Permutation groups, Cyclic groups, Coset decomposition, Lagrange theorem and its consequences,	10-15
Unit III	Normal subgroups, Quotient group, Homomorphism and Isomorphism, Fundamental theorems of homomorphism, Cayley's theorem.	12-15

Unit IV	Automorphism and inner automorphism, Automorphism groups and their computation, Normalizer and center of group, Finite groups, Commutator subgroups.	12-15
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Books recommended:

I. N. Herstein: *Topics in Algebra*, John Wiley & Sons, 2006.

Joseph A. Gallian: *Contemporary Abstract Algebra*, Narosa Publishing House, 2016.

David S. Dummit and Richard M. Foote: *Abstract Algebra*, John Wiley & Sons, 2011.

Surjeet Singh and Qazi Zameeruddin: *Modern Algebra*, Vikas Publishing House, India, 2021.

Further Readings:

Michael Artin: *Algebra*, Pearson Education, 2015.

N. Jacobson: *Lectures in Abstract Algebra-Vol. I, II & III*, Springer, 2013.

N. Jacobson: *Basic Algebra-Vol. I & II*, Dover Publications Inc., 2009.

R. S. Aggarwal: *A Textbook on Modern Algebra*, S Chand & Company, 1973.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-V

Bachelor of Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC COURSE (DSC Maths5)- Analysis

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths5: Analysis	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSC Maths3 and DSC Maths4

Bachelor of Science (Mathematics as one of the major Subject)

Programme :	<i>Bachelor of Science (Mathematics as one of the major Subject)</i>	Year: III	Semester: V Paper: DSC Maths5
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Subject: Mathematics

Course: DSC Maths5 **Course Title:** Analysis

Course Outcomes: The core concepts of Real analysis have been included in this course with a view that students can understand the behavior of real numbers and real valued functions in a critical way.

Credits: 4 Discipline Specific Course

Max. Marks: As per Univ. rules Min. Passing Marks: As per Univ. rules

Unit **Content** **Number of Hours**

Unit I	Topology of Real line: Complete ordered field, Archimedean Property, Supremum, infimum, Neighbourhood of a point, Interior of a set, open set, closed set, Derived set, Closure of a set, Bolzano-Weierstrass Theorem, Brief introduction of compactness and connectedness.	10-15
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Unit II	Integration: Riemann integral-definition and properties, Integrability of continuous and monotonic functions, Fundamental theorem of Calculus, Improper integrals and their convergence.	12-15
Unit III	Limit, continuity and differentiability of functions of a complex variable , Cauchy-Riemann equations, Analytic functions, Harmonic conjugates and Harmonic functions.	12-15
Unit IV	Line Integration, Cauchy's theorem, Cauchy's integral formula, Taylor's series, Laurent's series, Poles and singularities. Residues, The Residue theorem, Evaluation of Improper real integrals.	12-15

Books Recommended:

Walter Rudin: *Principle of Mathematical Analysis*, McGraw Hill Edition, 1976.

R. G. Bartle and D. R. Sherbert: *Introduction to Real Analysis*, John Wiley & Sons, 1999.

T. M. Apostol: *Mathematical Analysis*, Narosa Publishing House, New Delhi, 1985.

Further Readings:

Richard R. Goldberg: *Methods of Real Analysis*, John Wiley & Sons, 1976.

James R. Munkres: *Analysis on Manifolds*, Addison-Wesley Publishing Company, Advanced Book Program, Redwood City, CA, 1991.

H. L. Royden: *Real Analysis*, Macmillan Publishing Company, New York, 1988.

G. F. Simmons: *Introduction to Topology and Modern Analysis*, McGraw Hill Edition, 2011.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-V

Bachelor of Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths3)- Ring Theory

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths3: Ring Theory	4	3	2	0	Passed Class XII with Mathematics	Completed DSE Maths1

Bachelor of Science (Mathematics as one of the major Subject)

Programme : *Bachelor of Science (Mathematics as one of the major Subject)* Year: III Semester: V
Paper: DSE Maths3

Subject: Mathematics

Course: DSE Maths3 Course Title: Ring Theory

Course Outcomes: This course is useful to understand the concepts of algebraic structures and their properties. It will help the students for better understanding of other subjects, especially atomic structures in chemistry and certain concepts of physics.

Credits: 4 Discipline Specific Elective

Max. Marks: As per Univ. rules Min. Passing Marks: As per Univ. rules

Unit Content Number of Hours

Unit I Rings and their examples, Sub rings, Commutative rings, Divisors of zero, Integral domain, Inverse of an element in a ring, Field. 10-15

Unit II Skew field, Ideals, Characteristic of a ring, Ring Homomorphism, Quotient rings. 12-15

Unit III	Principal ideals, Maximal ideals, Prime ideals, Principal ideal domains, Polynomial rings and irreducibility.	12-15
Unit IV	Field of quotients of an integral domain, Embedding of an integral domain in a field, Factorization in an integral domain.	12-15

Books recommended:

I. N. Herstein: *Topics in Algebra*, John Wiley & Sons, 2006.

Joseph A. Gallian: *Contemporary Abstract Algebra*, Narosa Publishing House, 2016.

David S. Dummit and Richard M. Foote: *Abstract Algebra*, John Wiley & Sons, 2011.

Surjeet Singh and Qazi Zameeruddin: *Modern Algebra*, Vikas Publishing House, India, 2021.

Further Readings:

Michael Artin: *Algebra*, Pearson Education, 2015.

N. Jacobson: *Lectures in Abstract Algebra-Vol. I, II & III*, Springer, 2013.

N. Jacobson: *Basic Algebra-Vol. I & II*, Dover Publications Inc., 2009.

R. S. Aggarwal: *A Textbook on Modern Algebra*, S Chand & Company, 1973.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VI

Bachelor of Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC COURSE (DSC Maths6)- Vector spaces and linear transformations

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths6: Vector spaces and linear transformations	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSC Maths5

Bachelor of Science (Mathematics as one of the major Subject)

Programme :	<i>Bachelor of Science (Mathematics as one of the major Subject)</i>	Year: III	Semester: VI Paper: DSC Maths6
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Subject: Mathematics

Course: DSC Maths6	Course Title: Vector spaces and linear transformations
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Course Outcomes: Upon successful completion of this course, the students will be able to understand the theory used to solve the mathematical problems. It also helps to enhance the critical thinking of the students.

Credits: 4		Discipline Specific Course
Max. Marks: As per Univ. rules		Min. Passing Marks: As per Univ. rules
Unit	Content	Number of Hours
Unit I	Vector space, subspaces, Linear combinations, linear spans, Sums and direct sums, Linear dependence and independence, Bases and dimensions, Dimensions and subspaces, Coordinates and change of bases.	12-15

Unit II	Linear transformations, rank-nullity theorem, Linear operators, Invertible linear transformations, Matrix representation of a linear transformation, Transpose of a linear transformation, Similarity of Matrices, Linear functional, Dual space and dual basis, Second dual space, hyperspace.	12-15
Unit III	Eigen values and Eigen vectors, Algebraic and Geometrical Multiplicity, Characteristic and Minimal Polynomials, Annihilators, Cayley-Hamilton theorem, Similar Matrices, Diagonalizable operator.	10-15
Unit IV	Invariant Subspaces, Direct sum decomposition, Projection on a vector space, Primary decomposition theorem, Canonical Forms, Diagonal forms, Triangular forms, Jordan forms.	10-15

Books Recommended:

K. Hoffman and R. Kunze: *Linear Algebra*, Prentice Hall of India, 1972.

K. B. Dutta: *Matrix and Linear Algebra*, Prentice Hall of India, 2004.

Seymour Lipschutz and Marc L. Lipson: *Linear Algebra*, Schaum's Outline Series, McGraw Hill Edition, 2017.

S. H. Friedberg, A. J. Insel and L. E. Spence: *Linear Algebra*, Pearson Education, 2015.

Further Readings:

G. Hadley: *Linear Algebra*, Narosa Publishing House, 2002.

H. Helson: *Linear Algebra*, Hindustan Book Agency, New Delhi, 1994.

Gilbert Strang: *Linear Algebra and its Applications*, Cengage Learning India, 2005.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VI

Bachelor of Science (Mathematics as one of the major Subject)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths4)- Differential Equations

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths4: Differential Equations	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSC Maths3 and DSC Maths4

Bachelor of Science (Mathematics as one of the major Subject)

Programme :	<i>Bachelor of Science (Mathematics as one of the major Subject)</i>	Year: III	Semester: VI Paper: DSE Maths4
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Subject: Mathematics

Course: DSE Maths4	Course Title: Differential Equations
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Course Outcomes: This paper provides detailed knowledge of differential equations and their solutions. This course is useful for the students to solve not only mathematical problems in daily life but also helps to understand typical problems of physics and other related areas.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
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Unit I	Order and Degree of Differential Equations, Complete primitive (general solution, particular solution and singular solutions), Existence and uniqueness of the solution $dy/dx = f(x,y)$. Differential equations of first order and first degree, Separation of variables, Homogeneous Equations, Linear Differential Equations, Exact Differential Equations, Integrating Factor, Equation of First order but not of first degree, variation of parameters, Clairaut's form, Singular solutions, Trajectory, Orthogonal Trajectory, Self-Orthogonal family of Curves.	12-15
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Unit II	Linear Differential Equations: Linear equations with constant coefficients, Complementary function, Particular integral, working rule for finding solution, Homogeneous linear equations. Linear differential equations of second order with variable coefficients.	12-15
Unit III	Miscellaneous Equations: Simultaneous differential equations, Differential equations of the form $dx/P = dy/Q = dz/R$ where P, Q, R are functions of x, y and z, Exact differential equations, Total differential equations, Series solutions of differential equations,	12-15
Unit IV	Laplace Transformation, Inverse Laplace Transformation, Applications to solve Differential equations	10-15

Books Recommended:

G. F. Simmons: *Differential Equations with Application and Historical Notes*, McGraw Hill Edition, 2002

Shepley L. Ross: *Differential Equations*, John Wiley & Sons, 1984.

M. D. Raisinghania: *Ordinary & Partial Differential Equation*, S. Chand & Co. Ltd, 2017.

B. Rai, D. P. Choudhary and H. J. Freedman: *A Course of Ordinary Differential Equations*, Narosa, 2002.

Further Readings:

Earl A. Coddington and Norman Levinson: *Theory of Ordinary Differential Equations*, McGraw-Hill Edition, 1998.

Ravi P. Agarwal and Donal O'Regan: *Ordinary and Partial Differential Equations*, Springer, 2009.

Martin Braun: *Differential Equations and Their Applications*, Springer, 1993.

Erwin Kreyszig: *Advanced Engineering Mathematics*, John Wiley & Sons, 2011.

Ian N. Snedden: *Elements of Partial Differential Equations*, Dover Publication, 2013.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VII
Bachelor of Science (Honors)

DISCIPLINE SPECIFIC COURSE (DSC Maths7)- Real Analysis

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths7: Real Analysis	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSC Maths5

Bachelor of Science (Honors)

Programme :	<i>Bachelor of Science (Honors)</i>	Year: IV	Semester: VII Paper: DSC Maths7
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Subject: Mathematics

Course: DSC Maths7	Course Title: Real Analysis
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Course Outcomes: The core concepts of Real Analysis has been included in this course with a view that students can understand the behavior of different sets with respect to metric or distance function.

Credits: 4	Discipline Specific Course
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
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Unit I	Metric spaces: metric, Various examples, of metric spaces, open sets, interior of a set, Structure of open subsets of the real line, limit points, closed sets, closure of a set, Cauchy sequences, completeness.	12-15
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Unit II	Functions of several variables: Concept of functions of two variables, Simultaneous and iterated limits in functions of two variables, Partial derivatives: Definition, Existence and continuity, Interchange of order of differentiation, Directional derivatives.	12-15
Unit III	Composite functions, Linear Continuity of function of two variables, differentiability of functions of two variables, Taylor's Theorem.	10-15
Unit IV	Linear transformation, Vector Valued functions, Differentiation of vector valued functions, inverse function theorem, implicit function theorem.	10-15

Books Recommended:

S. C. Malik and Savita Arora: Mathematical Analysis, New Age International.

G.F. Simmons: Introduction to Topology and Modern Analysis, Tata McGraw Hill.

T. M. Apostol: Mathematical Analysis, Narosa Publishing House, New Delhi, 1985.

Further Readings:

W. Rudin: Principles of Mathematical Analysis (3rd edition), Tata Mc Graw Hill Kgakusha, International Student Edition, 1976.

Richard R. Goldberg: Methods of Real Analysis, John Wiley & Sons, 1976.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VII
Bachelor of Science (Honors)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths5)- Topology

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths5: Topology	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Bachelor of Science (Honors)

Programme :	<i>Bachelor of Science (Honors)</i>	Year: IV	Semester: VII Paper: DSE Maths5
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Subject: Mathematics

Course: DSE Maths5	Course Title: Topology
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Course Outcomes: This course is useful to open up a new direction to view different shapes and other mathematical objects. This course helps to understand the concepts of topologies on a set and their properties. It will help the students for better understanding of mathematical and other disciplines of physical and natural sciences.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Basic concepts in Topology: Topology on a set, a topological space with examples, topologies on the real number system.	10-15
Unit II	Neighborhood of a point/set, Open and closed sets, interior, boundary, closure, limit point, Derived sets of a set, Base and sub-base of a topology, Separable Spaces, First and Second Countable spaces.	12-15

Unit III	Continuous map, open and closed maps, homeomorphisms, Topological invariants, Pasting Lemma, Subspaces, product spaces, quotient space.	10-15
Unit IV	Compactness, Compact spaces, Compactness of a metric space, Connectedness, connected space, components. Separation axioms: $T_1, T_2, T_3, T_{3\frac{1}{2}}, T_4$, regular, completely regular and normal space.	12-15

Books Recommended:

J. R. Munkres: Topology: Narosa Publishing House.

Shaum's outlines series: Tata McGraw Hill.

K. D. Joshi: Introduction to General Topology, Wiley Eastern, 1983.

M. D. Raisinghania & R. S. Aggarwal: Topology, S. Chand & Co.

Further Readings:

G. F. Simmons: Introduction to Topology and Modern Analysis, McGraw Hill, 1963.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VII
Bachelor of Science (Honors)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths6)- Differential Geometry

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths6: Differential Geometry	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Bachelor of Science (Honors)

Programme :	<i>Bachelor of Science (Honors)</i>	Year: IV	Semester: VII Paper: DSE Maths6
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Subject: Mathematics

Course: DSE Maths6	Course Title: Differential Geometry
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Course Outcomes: This course is useful to understand the concepts of geometric structures and their properties using differential calculus. It will help the students for better understanding of other subjects, especially atomic structures in chemistry and certain concepts of physics.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Curve in space, parameterized curves, regular curves, helices, arc length, reparameterization (by arc length), Tangent, principal normal, binormal, osculating plane, normal plane, rectifying plane, curvature torsion of smooth curves, Frenet- Serret formulae, Frenet approximation of space curve.	12-15
Unit II	Order of contact, osculating circle, osculating sphere, Spherical indicatrices, involutes and evolutes, Bertrand	10-15

	Curves, intrinsic equations of space curves, isometries of R^3 , Fundamental theorem of space curves, surfaces in R^3 .	
Unit III	Regular Surfaces, coordinates neighborhoods, parameterized surfaces, change of parameters, level sets of smooth functions on R^3 , surfaces of revolution, mean curvature, tangent vector, first and second fundamental forms, classification of points on a surface	12-15
Unit IV	Curvature of curve on surfaces, normal curvature, Meusnier theorem, principle curvatures, geometric interpretation of principal curvatures, Euler theorem, mean curvature, line of curvature, Rodrigue's formula, umbilical points, minimal surfaces, definition and examples, Gaussian curvature.	12-15

Books Recommended:

D. Somasundaram: Differential Geometry, A First Course, Narosa Publishing House, New Delhi, 2005.

Andrew Pressley: Elementary Differential Geometry, Springer (Undergraduate Mathematics Series), 2001.

T.J.Willmore: An Introduction To Differential Geometry, Oxford University Press.

Further Readings:

J. A. Thorpe: Elementary Topics in Differential Geometry, Springer (Undergraduate Texts in Mathematics), 1979.

B.O.Niell: Elementary Differential Geometry, Academic Press.

Do Carmo : Curves and surfaces,

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VII
Bachelor of Science (Honors)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths7)- Dynamics of Rigid Bodies

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths7: Dynamics of Rigid Bodies	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Bachelor of Science (Honors)

Programme :	<i>Bachelor of Science (Honors)</i>	Year: IV	Semester: VII Paper: DSE Maths7
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Subject: Mathematics

Course: DSE Maths7	Course Title: Dynamics of Rigid Bodies
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Course Outcomes: This course is useful to understand the concepts of motion of rigid bodies. It will help the students for better understanding of the other subjects, especially in engineering and certain concepts of physics.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	D'Alembert's principle, Motion about a fixed axis (Finite and Impulsive forces).	10-15
Unit II	Motion in two dimensions under Finite and Impulsive forces, Principle of conservation of momentum and energy.	12-15
Unit III	Lagrange's equations in generalized co-ordinates.	10-15

Unit IV	Hamilton's principle, principle of least action, Euler's geometrical and dynamical equations.	12-15
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Books Recommended:

Bhu Dev Sharma: Dynamics of Rigid Bodies, Kedarnath Ramnath Sons, 1984.

M. Ray & Harswarup Sharma: A text book of Dynamics of Rigid Body, Students' Friends &Co., Agra-2, 1971.

H. Goldstein: Classical Mechanics, Narosa, 1990.

Further Readings:

S. L. Loney: Dynamics of rigid bodies.

A. S. Ramsey: Dynamics – Part II.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VIII
Bachelor of Science (Honors)

DISCIPLINE SPECIFIC COURSE (DSC Maths8)- Complex Analysis

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths8: Complex Analysis	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSC Maths5

Bachelor of Science (Honors)

Programme :	<i>Bachelor of Science (Honors)</i>	Year: IV	Semester: VIII Paper: DSC Maths8
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Subject: Mathematics

Course: DSC Maths8	Course Title: Complex Analysis
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Course Outcomes: Upon successful completion of this course, the students will be able to understand the theory used to solve the mathematical problems. It also helps to enhance the critical thinking of the students.

Credits: 4	Discipline Specific Course
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
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Unit I	Conformal mappings, Power series representation of analytic functions, Analytic functions as mappings, Riemann sphere, Linear transformations, Mobius transformation, Cross ratios, Mobius transformation on circles.	12-15
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Unit II	Derivative of an analytic function, Higher order derivatives, Cauchy's theorem integral formula. Morera's theorem, Cauchy inequality and Liouville's theorem.	12-15
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Unit III	Counting zeros, The open mapping theorem, Maximum modulus principle, Schwarz lemma, The fundamental theorem of algebra.	12-15
Unit IV	Entire functions, Hadmard's three circle theorem, Jensen's formula, Meromorphic functions.	12-15

Books Recommended:

J. B. Conway: *Functions of One Complex Variable*, Narosa Publishing House, 1980.

R. V. Churchill and J. W. Brown and R. F. Verhey: *Complex Variables and Applications*, McGraw Hill Edition, 1976.

Further Readings:

L. V. Ahlfors: *Complex Analysis*, McGraw Hill Edition, 1977.

E. T. Copson: *Complex Variables*, Oxford University Press.

Richard R. Goldberg: *Methods of Real Analysis*, John Wiley & Sons, 1976.

D. Sarason: *Complex Function Theory*, Hindustan Book Agency, Delhi, 1994.

James R. Munkres: *Analysis on Manifolds*, Addison-Wesley Publishing Company, Advanced Book Program, Redwood City, CA, 1991.

H. L. Royden: *Real Analysis*, Macmillan Publishing Company, New York, 1988.

G. F. Simmons: *Introduction to Topology and Modern Analysis*, McGraw Hill Edition, 2011.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VIII
Bachelor of Science (Honors)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths8)- Algebra

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths8: Algebra	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Bachelor of Science (Honors)

Programme :	<i>Bachelor of Science (Honors)</i>	Year: IV	Semester: VIII Paper: DSE Maths8
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Subject: Mathematics

Course: DSE Maths8	Course Title: Algebra
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Course Outcomes: This course will help students to understand the concept of algebraic structures especially groups and rings.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Normal and subnormal series, composition series, Jordan Holder theorem, chain conditions.	12-15
Unit II	Commentators. Solvable groups, solvability of subgroups and factor groups. Nilpotent groups and their equivalent characterizations.	13-15
Unit III	Rings, ideals, prime and maximal ideals, quotient rings. Factorization theory in commutative domains. Prime and irreducible elements, Euclidean Domains. Principal Ideal Domain. Divisor chain condition. Unique Factorization Domains, Polynomial rings over domains. Eisenstein's	15-18

	irreducibility criterion. Unique factorization in polynomial rings over UFDs.	
Unit IV	Fields, finite fields, field extensions, Galois extensions.	10-15

Books Recommended:

J. Gallian: Abstract Algebra, Narosa Publication.

Ramji Lal: Fundamentals in Abstract Algebra, Chakra Prakashan, Allahabad, 1985.

I. N. Herstein: Topics in Algebra, Wiley Eastern Ltd., N.D., 1975.

Further Readings:

M. Artin: Algebra, Prentice Hall of India.

N. Jacobson: Basic Algebra, Vol. I, Hindustan Publishing Co., New Delhi.

D. S. Dummit and R. M. Foote: Abstract Algebra, John Wiley, N. Y.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VIII
Bachelor of Science (Honors)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths9)- Partial Differential Equations

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths9: Partial Differential Equations	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Bachelor of Science (Honors)

Programme : <i>Bachelor of Science (Honors)</i>	Year: IV	Semester: VIII Paper: DSE Maths9
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Subject: Mathematics

Course: DSE Maths9	Course Title: Partial Differential Equations
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Course Outcomes: To solve any real-world problem mathematically, differential equations are widely used. This course will help students to deal with such problems and use differential equations to solve them.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
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Unit I	Existence and uniqueness of solutions of initial value problems for first order ordinary differential equations, singular solutions of first order ODEs, system of first order ODEs., General theory of homogeneous and non-homogeneous linear ODEs, variation of parameters, Sturm-Liouville boundary value problem, Green's function.	10-15
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Unit II	Formation of PDEs, First order PDEs, Complete, general and singular integrals, Lagrange's or quasi-linear equations, Integral surfaces through a given curve.	12-15
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	Orthogonal surfaces to a given system of surfaces, Characteristic curves.	
Unit III	Pfaffian differential equations, Compatible systems, Charpit's method, Jacobi's Method. Cauchy problem for first order PDEs.	12-15
Unit IV	Linear equations with constant coefficients, Reduction to canonical forms, Classification of second order PDEs, General solution of higher order PDEs with constant coefficients.	10-15

Books Recommended:

G. F. Simmons: Differential Equations with Application and Historical Notes, McGraw Hill Edition, 2002

Shepley L. Ross: Differential Equations, John Wiley & Sons, 1984.

M. D. Raisinghania: Ordinary & Partial Differential Equation, S. Chand & Co. Ltd, 2017.

B. Rai, D. P. Choudhary and H. J. Freedman: A Course of Ordinary Differential Equations, Narosa, 2002.

Further Readings:

Earl A. Coddington and Norman Levinson: Theory of Ordinary Differential Equations, McGraw-Hill Edition, 1998.

Ravi P. Agarwal and Donal O'Regan: Ordinary and Partial Differential Equations, Springer, 2009.

Martin Braun: Differential Equations and Their Applications, Springer, 1993.

Erwin Kreyszig: Advanced Engineering Mathematics, John Wiley & Sons, 2011.

Ian N. Snedden: Elements of Partial Differential Equations, Dover Publication, 2013.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-VIII
Bachelor of Science (Honors)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths10)- Tensor Calculus

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths10: Tensor Calculus	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Bachelor of Science (Honors)

Programme : <i>Bachelor of Science (Honors)</i>	Year: IV	Semester: VIII Paper: DSE Maths10
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Subject: Mathematics

Course: DSE Maths10	Course Title: Tensor Calculus
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Course Outcomes: The core concepts of tensors have been included in this course with a view that students will be benefitted by the algebra of tensors. This helps students to understand various courses like Einstein's theory of Relativity, Image processing etc.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	n-dimensional real vector space, transformation of coordinates, invariants, contravariant and covariant vectors, tensors of order two: contravariant tensors, covariant tensors and mixed tensors, higher order tensors, operations on tensors: addition, subtraction, multiplication, contraction and inner product.	10-15
Unit II	Symmetric and skew symmetric tensors, quotient law of tensors, relative tensors.	10-15

Unit III	metric tensor, length of a curve, magnitude of vector, angle between two vectors, associated tensors, conjugate symmetric tensors,	12-15
Unit IV	Christoffel symbols, transformation rule and group property, covariant derivative, intrinsic derivative, Gradient, divergence and curl.	13-15

Books Recommended:

N. Islam: Tensors and their applications, New Age International Publishers, 2006.

C.E. Weatherburn: Riemannian Geometry and Tensor Calculus.

B. Spain: Tensor Calculus.

Further Readings:

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-IX

Master of Science (Mathematics)

DISCIPLINE SPECIFIC COURSE (DSC Maths9)- Linear Algebra

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths9: Linear Algebra	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSC Maths5

Master of Science (Mathematics)

Programme : <i>Master of Science (Mathematics)</i>	Year: V	Semester: IX Paper: DSC Maths9
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Subject: Mathematics

Course: DSC Maths9	Course Title: Linear Algebra
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Course Outcomes: The core concepts of Linear Algebra have been included in this course with a view that students can understand the behavior of mathematical entities called vector spaces.

Credits: 4	Discipline Specific Course
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	A brief review of vector space, Inner products, Orthogonality, Best approximations, Projections, Cauchy-Schwartz inequality.	12-15
Unit II	Adjoint of a linear transformation, Self-adjoint transformations, Unitary operators.	12-15
Unit III	Normal operators: Definition and properties, Spectral theorem.	10-15

Unit IV	Eigen vectors and eigen values of a linear operator, Minimal polynomial of a linear operator and its relations to characteristic polynomial, Caley-Hamilton theorem.	10-15
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Books Recommended:

K. Hoffman and R. Kunze: *Linear Algebra*, Prentice Hall of India, 1972.

K. B. Dutta: *Matrix and Linear Algebra*, Prentice Hall of India, 2004.

Seymour Lipschutz and Marc L. Lipson: *Linear Algebra*, Schaum's Outline Series, McGraw Hill Edition, 2017.

S. H. Friedberg, A. J. Insel and L. E. Spence: *Linear Algebra*, Pearson Education, 2015.

Further Readings:

G. Hadley: *Linear Algebra*, Narosa Publishing House, 2002.

H. Helson: *Linear Algebra*, Hindustan Book Agency, New Delhi, 1994.

Gilbert Strang: *Linear Algebra and its Applications*, Cengage Learning India, 2005.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-IX

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths11)- Measure Theory

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths11: Measure Theory	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: IX Paper: DSE Maths11
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Subject: Mathematics

Course: DSE Maths11	Course Title: Measure Theory
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Course Outcomes: The core concepts of measure and integration have been included in this course with a view that students can understand the measure of sets and summation over the sets.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Countable sets, uncountable sets, relation between the cardinality of a nonempty set and the cardinality of its power set; Boolean ring, σ -ring, Boolean algebra and σ -algebra of sets, Set function.	12-15
Unit II	Introduction, Outer measure, Measurable sets and Lebesgue measure, Example of non-measurable sets, Measurable functions.	10-15

Unit III	The Riemann integral, The Lebesgue integral of a bounded function over a set of finite measure, The integral of nonnegative functions. The general Lebesgue integral, Convergence in measure.	12-15
Unit IV	Differentiation of monotone functions, Functions of bounded variation, Differentiation of an integral, Absolute continuity, Convex functions.	10-15

Books Recommended:

P. K. Jain: Measure Theory, New Age International.

P. R. Halmos: Measure Theory, Grand Text Mathematics, 14 Springer, 1994.

I. K. Rana: An Introduction to Measure and Integration, (Second Edition), Narosa Publishing House, New Delhi, 2005.

Further Readings:

E. T. Copson: Complex Variables, Oxford University Press. K.R. Parthasarathy: Introduction to Probability and Measure, TRIM 33, Hindustan Book Agency, New Delhi, 2005.

E. Hewit and K. Stromberg: Real and Abstract Analysis, Springer, 1975.

H. L. Royden: Real Analysis, Macmillan Publishing Company, New York, 1988.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-IX

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths12A)- Mathematical Statistics

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths12A: Mathematical Statistics	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: IX Paper: DSE Maths12A
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Subject: Mathematics

Course: DSE Maths12A	Course Title: Mathematical Statistics
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Course Outcomes: Upon completion of this course, students will be enabled to apply statistical methods in addition to various mathematical methods.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Descriptive Statistics: Measures of central tendency, dispersion skewness and kurtosis Elements of probability: Sample space, discrete probability, independent events, Baye's theorem, random variables and distribution functions (univariate, bivariate, and generalization to multivariate).	10-15
Unit II	Mathematical expectation and moments: Moment generating function, Characteristic function and cumulants. Probabilistic inequalities. Modes of convergence: weak and strong laws of large numbers. Central limit theorem (i.i.d. case). Markov chains with	12-15

	finite and countable state space, Poisson and birth- and-death processes.	
Unit III	Some standard discrete and continuous univariate distributions (Binomial, Poisson, Normal, Gamma and Beta), Distribution of order statistics and range.	10-15
Unit IV	Correlation, Rank correlation. Regression lines. Multiple and partial correlation of three variables only, Data reduction techniques: Principal component analysis, discriminant analysis, cluster analysis, canonical correlation.	12-15

Books Recommended:

M.G.Kendall: Advanced theory of statistics Vol. I &II, Charle's Griffiin & Co.

R. Hogg and A Craig: Introduction to Mathematical Statistics, Mac Millan & Co.

C.E. Weatherbun: A first course in Mathematical Statistics, The English Language Book Society And Cambridge University Press, 1961.

S.C. Gupta & V.K. Kapoor: Fundamentals of Mathematical Statistics, Sultan Chand & Co

Further Readings:

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-IX

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths12B)- Number Theory

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths12B: Number Theory	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: IX Paper: DSE Maths12B
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Subject: Mathematics

Course: DSE Maths12B	Course Title: Number Theory
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Course Outcomes: The core concepts of numbers have been included in this course with a view that students can understand the behavior of prime numbers and natural numbers in a critical way.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Prime Numbers, Unique Factorization theorem, Farey series, Irrational numbers, Congruences, Residues, Quadratic Reciprocity Law, Primitive roots.	8-10
Unit II	Fermet's theorem, Wilson's theorem, Continued fractions, Approximation of irrational of rationals, Hurwitz theorem.	10-12
Unit III	The fundamental theorem of arithmetic in $K(1)$, $K(i)$, $K(\rho)$, Diophantine equation $X^2 + Y^2 = Z^2$, $X^4 + Y^4 = Z^4$, $aX^2 + bY^2 + cZ^2 = 0$, Quadratic fields, The arithmetic functions:	10-12

Unit IV	$d(n)$, $\sigma(n)$, $\mu(n)$ and $\varphi(n)$ including elementary result on their order and average order.	10-12
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Books Recommended:

G. H. Hardy and E. M. Wright: Introduction to the theory of numbers, Oxford University Press, 4th Edition.

D. M. Burton: Elementary Number Theory, 6th Edition, Tata McGraw Hill.

Thomas Koshy: Elementary Number Theory with Applications, Academic Press, 2nd Edition.

Kenneth H. Rosen: Elementary Number Theory and its Applications, Addison-Wesley Publishing Company, 1986.

Further Readings:

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-IX

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths13A)- Fluid Dynamics

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths13A: Fluid Dynamics	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: IX Paper: DSE Maths13A
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Subject: Mathematics

Course: DSE Maths13A	Course Title: Fluid Dynamics
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Course Outcomes: This course will enable students to understand how the motion of fluids is studied using mathematical tools.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Lagrangian and Eulerian methods, Equation of continuity, Boundary surface, Stream lines, Velocity potential, Euler's equation of motions, Bernoulli's theorem, Helmholtz equations, Cauchy's integral, Equation of action under impulsive forces, Principal of energy.	10-15
Unit II	Motion in two dimensions, Velocity potential and current functions, Sources and sinks, Doublet and images, Circle theorem, Motion of circular and elliptic cylinder in two dimensions, Joukowski transformation, Motion in three dimensions, Three dimensional sources, Sinks and	12-15

	doublets, Image of source in front of sphere, Motion of spheres, Stroke's stream function.	
Unit III	General theory of irrotational motion, Permanence of irrotational motion circulation, Stroke's theorem, Kelvin's circulation theorem, Green's theorem, Kelvin's minimum energy theorem, Conformal Representation, Kutta and Joukowski transformation, Theorems of Schwartz Christoffel.	12-15
Unit IV	Vortex motion: Rectilinear vortices, Rectilinear vortex with a circular section, An infinite row of parallel rectilinear vortices, Karman stream, Use of conformal transformation, Vortex pairs.	10-15

Books Recommended:

A. S. Ramsey: A Treatise on Hydrodynamics.

W. H. Besant and A. S. Ramsey: A Treatise on Hydrodynamics, CBS Publisher and Distributors, Delhi, 1988.

M. D. Raisinghania: Fluid Dynamics, S. Chand, 1939

Further Readings:

F. Chorlton: A Text Book of Fluid Dynamics, CBC, 1985.

S. W. Yuan: Foundations of Fluid Dynamics, Prentice-Hall of India, 1988.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-IX

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths13B)- Discrete Mathematics

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths13B: Discrete Mathematics	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: IX Paper: DSE Maths13B
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Subject: Mathematics

Course: DSE Maths13B	Course Title: Discrete Mathematics
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Course Outcomes: This course will enable students to understand various concepts which are useful for higher study in other disciplines of mathematical sciences like computer science, data science etc.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Principle of mathematical induction, partially ordered sets, Lattices: Lattices as partially ordered sets, Their Properties, Lattices and algebraic systems. Principle of duality, Sub lattices, Complete, Complemented and Distributive lattices.	12-15
Unit II	Boolean algebra, Boolean functions, Boolean expressions, Applications to switching circuits.	10-15
Unit III	Elements of graph theory: Basic terminology, Paths and circuits, Eulerian and Hamiltonian graphs, planar graphs, Directed graphs.	12-15

Unit IV	Trees: Rooted trees, path lengths, spanning trees, minimum spanning trees.	12-15
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Books Recommended:

C. L. Liu: Elements of discrete mathematics, Tata McGraw Hill Education, 2008.

Ram Babu: Discrete Mathematics, Pearson Edition India, 2011.

Lipschutz: Discrete Mathematics, Tata McGraw Hill, 2011.

Further Readings:

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-X

Master of Science (Mathematics)

DISCIPLINE SPECIFIC COURSE (DSC Maths10)- Functional Analysis

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSC Maths10: Functional Analysis	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSC Maths5

Master of Science (Mathematics)

Programme : <i>Master of Science (Mathematics)</i>	Year: V	Semester: X Paper: DSC Maths10
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Subject: Mathematics

Course: DSC Maths10	Course Title: Functional Analysis
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Course Outcomes: The core concepts of Functional Analysis have been included in this course with a view that students can understand the behavior of functions on vector spaces.

Credits: 4	Discipline Specific Course
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
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Unit I	Metric convergence of sequences, Normed spaces, Banach Space, Properties of Normed spaces, Finite dimensional normed spaces and subspaces; Compactness and finite dimension, linear operators, Bounded and continuous linear operators; Linear functional; linear operators and functional on finite dimensional spaces, Normed spaces of operators, Dual space.	12-15
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Unit II	Inner product space; Hilbert space; Properties of Inner product spaces, Orthogonal complements and direct sums, Orthonormal sets and sequences; Hilbert adjoint operators, Self-Adjoint, Unitary and normal operators.	12-15
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Unit III	Fundamental Theorems of Normed and Banach Space: Zorn's Lemma, Hahn Banach Theorem, Hahn Banach Theorem for complex vector spaces and normed spaces, Applications to bounded linear functionals on $C[a, b]$, Adjoint operators, Uniform boundedness theorem, strong and weak convergence, convergence of sequences of operators and functional, Applications of summability of sequences, Open mapping theorem and closed graph theorem.	10-15
Unit IV	Banach contraction principle, Applications of Banach's theorem to linear, differential and integral equations, Approximation in Normed spaces, Uniqueness, strict convexity, Uniform approximation, approximation in Hilbert spaces.	12-15

Books Recommended:

Erwin Kreyszig: Introductory Functional Analysis, Wiley India edition.

G. F. Simmons: Introduction to Topology and Modern Analysis, McGraw Hill, 1963.

A. E. Taylor: Introduction to Functional Analysis, John Wiley, 1958.

R. E. Edwards: Functional Analysis, Holt Rinehart and Winston, 1965

Further Readings:

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-X
Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths14)- Numerical Methods

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths14: Numerical Methods	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme : <i>Master of Science (Mathematics)</i>	Year: V	Semester: X Paper: DSE Maths14
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Subject: Mathematics

Course: DSE Maths14	Course Title: Numerical Methods
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Course Outcomes: This course will help students to extend their understanding of mathematical tools and they will be able to use new methods of problem solving.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
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Unit I	Errors in numerical Calculations: Absolute, Relative, Percentage errors, General Error, Error in series approximation. Solutions of Algebraic and Transcendental Equation: Bisection method, false position method, Newton-Raphson and generalized Newton's Method, Graffe's root squaring method, Lin Bairstow's method, Picards iteration method, convergence and error estimates of iterative methods.	10-15
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Unit II	Linear systems of equations: Consistency of Linear System of equations, Solutions of Linear Systems by direct method: Gaussian elimination and computation of inverse of a matrix, Method of Factorization, Solutions of	12-15
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	Tridiagonal systems and ill conditioned linear systems. Solutions of linear systems by iterative methods: Jacobi method, Gauss- Siedel method.	
Unit III	Interpolation and curve fitting: Errors in Polynomial interpolation, Finite differences, Differences of a polynomial, Newton's forward and backward interpolation, Central differences, Gauss, Stirling, Bessel's and Everett's Formulae, Practical interpolation and interpolation with unevenly spaced points, Lagrange's Interpolation formula, Divided difference and Newton's General interpolation formula, Least square curve fitting procedure.	10-15
Unit IV	Numerical differentiation and integration: Numerical differentiation, cubic Spline method, Maximum and minimum values of tabulated function, Newton-Cotes Integration formula, Numerical integration by Trapezoidal rule, Simpson's 1/3, Simpson's 3/8, Weddle's rule and Romberg Integration, Numerical solution of ODE by Picard's Euler's Modified Euler's and Runge-Kutta methods.	12-15

Books Recommended:

S. S. Sastry: Introductory Methods Numerical Analysis, Prentice- Hall of India.

C.F. Gerald and P. O. Wheatley: Applied Numerical Analysis, Addison- Wesley, 1998. Further Readings:

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-X

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths15A)- Operations Research

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths15A: Operations Research	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: X Paper: DSE Maths15A
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Subject: Mathematics

Course: DSE Maths15A	Course Title: Operations Research
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Course Outcomes: This course will enable students to understand various methods for the solution of optimization problem.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
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Unit I	Basics of OR and LPP: Development of OR, Definition, characteristics, scope, objectives and limitations of OR, Formulation of LPP, Graphical Method to solve LPP, General LPP, Canonical and Standard forms, Properties of Solutions and Theory of Simplex method, Big M Method and Two phase simplex method, Degeneracy in LPP. Duality in LPP, Duality and simplex method, Dual simplex method, Revised simplex method and bounded variable problems.	12-15
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Unit II	Transportation Models: Lp Formulation of TP, Transportation Table, Finding initial basic feasible solution, Test of optimality, Degeneracy, MODI method, Stepping Stone method,	10-15
Unit III	Assignment Models: Solutions of Assignment problems, Hungarian method, Duality in assignment problem.	10-15
Unit IV	Sensitivity Analysis: Changes in Objective Function Coefficient, Changes in constants, Changes in coefficients of decision variables in constraints, Structural changes.	12-15

Books Recommended:

H. A. Taha: Operations Research, An Introduction, Pearson.

Kanti Swarup, P K Gupta, Manmohan: Operations Research, Sultan Chand & Sons, New Delhi.

S.S. Rao: Optimization Theory and Applications Wiley Eastern.

Further Readings:

F. S. Hiller and G. J. Lieberman: Introduction to Operation Research (6th Edition), McGraw-Hill International Edition, 1995.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-X

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths15B)- Relativity

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths15B: Relativity	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: X Paper: DSE Maths15B
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Subject: Mathematics

Course: DSE Maths15B	Course Title: Relativity
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Course Outcomes: The core concepts of Relativity have been included in this course with a view that students can understand the behavior of solar system and space in a critical way.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Special Relativity: Inertial Frames of reference, Michelson-Morley experiment, Doppler effect, Stellar aberration, Simultaneity, Postulates of special relativity, Lorentz transformation, Length contraction, Time dilation, Clock paradox, Addition of velocities and accelerations, Four-dimensional space time, Light cone, Mass variation, Velocity four vector, Momentum and force, Mass-Energy relationship.	10-15
Unit II	General Relativity: Geodesics, Geodesic coordinates, Curvature tensor and its algebraic properties, Bianchi's identities, Contracted curvature tensor, Conditions for a flat space time, Displacement of space –time, Killing	12-15

	equations, Groups of motion, Space –time of constant curvature.	
Unit III	Principal of covariance, Non-inertial frames of reference, Principal of equivalence, Weak field approximation of geodesic equations, Law of gravitation in empty space-time, Canonical coordinates, Schwarzschild solutions.	10-15
Unit IV	Experimental tests of general relativity, Schwarzschild metric in isotropic coordinates, Birkhoff's theorem, Law of gravitation in non-empty space time.	10-15

Books Recommended:

D.F. Lawden: An Introduction to tensor calculus and relativity,

J.V. Narlikar: General relativity and cosmology.

R.H. Good: Basic concept of relativity, 1978.

Further Readings:

A.S. Eddington: Mathematical theory of relativity, 1981.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-X

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths16A)- Special Functions

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths16A: Special Functions	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: X Paper: DSE Maths16A
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Subject: Mathematics

Course: DSE Maths16A	Course Title: Special Functions
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Course Outcomes: This course will extend the knowledge of functions to the students by adding the class of functions defined using integrals.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	Preliminaries, Gamma function and related functions, Gauss multiplication theorem, the hypergeometric differential equation, Gauss hypergeometric function.	10-15
Unit II	Integral representation of hypergeometric function, Evaluation of hypergeometric function, the confluent hypergeometric differential equation, Confluent hypergeometric function.	12-15
Unit III	Bessel's equation, solution of Bessel's equation, Bessel's functions $J_n(x)$, Recurrence Formulae, Equations reducible to Bessel's equation, orthogonality of Bessel's Functions, A generating function for $J_n(x)$, Basic properties.	12-15

Unit IV	Legendre's equation, Legendre's polynomial $P_n(x)$, Legendre's function of the second kind $Q_n(x)$, General solution of Legendre's equation, Rodrigue's formula, Legendre polynomials, A generating function of Legendre's polynomial, Orthogonality of Legendre	12-15
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Books Recommended:

E.D. Rainville: Special functions.

Nirvikar Saran: Special Functions.

W.W. Bell: Special Function for Scientists and Engineers, Dever publications, 2002,

U.P. Singh: Special Function & Their Application, WISDOM PRESS, 2012.

Further Readings:

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-X

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths16B)- Riemannian Geometry

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths16B: Riemannian Geometry	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: X Paper: DSE Maths16B
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Subject: Mathematics

Course: DSE Maths16B	Course Title: Riemannian Geometry
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Course Outcomes: This course is useful to view geometry of the space where our Euclidean geometry is not applicable. It will help the students for better understanding of other disciplines of physical and natural sciences.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	N-dimensional real vector space and its dual space, multilinear functions on vector spaces, tensor product, contravariant and covariant vectors, second order tensors, tensors of type (r,s). Algebraic Operations on tensors, Symmetric and skew symmetric properties, inner product of vectors, Euclidean vector space.	12-15
Unit II	Differentiable manifold, Lie-bracket, Tangent space, Connections, Covariant derivatives, Curvature tensor, Parallelism, Lie derivative, Exterior derivative, Cartan's structural equations.	12-15

Unit III	Riemannian geometry: Riemannian metric, Christoffel symbols, Curvature tensor with respect to Christoffel symbols, Differential operators, Geodesics, Geodesic coordinates, Riemannian curvature, Conformal curvature tensor, Frenet's formulae.	13-15
Unit IV	Sub-manifolds and Hypersurfaces: Normals, Gauss's formulae, Weingarten equations, Coordinate viewpoint, Lines of curvature, Generalized Gauss and Mainardi-Codazzi equations.	12-15

Books Recommended:

R.S. Mishra: A Course in tensors with applications to Riemannian Geometry, Pothishala Pvt. Ltd., Allahabad, 1965.

R. L. Bishop and S. I. Goldberg: Tensor Analysis on Manifolds, Dover Publications, New York.

S. S. Chern: Differentiable Manifolds, University of Chicago, Chicago.

Further Readings:

K. Yano: The theory of Lie derivatives and its applications, North-Holland Publishing Company, Amsterdam, 1957.

Matthew S. Smith: Principal and Application of Tensor Analysis, W. Sons (Indianapolis) 1963.

H.S. Shukla, Prasad & Dhruwa Narain Dubey: Differential Geometry of Manifolds, Vandana Prakashan, Mohanlalpur, Gorakhpur.

Digital Platform: NPTEL/SWAYAM/MOOCs.

Semester-X

Master of Science (Mathematics)

DISCIPLINE SPECIFIC ELECTIVE (DSE Maths16C)- Introduction to programming using MATLAB

No. of Hours: 50-60

CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course Title	Credits	Credit distribution of the Course			Eligibility criteria	Pre-requisite of the course (if any)
		Lecture	Tutorial	Practical/Practice		
DSE Maths16C: Introduction to programming using MATLAB	4	3	2	0	Passed diploma in Science with Mathematics	Completed DSE Maths3

Master of Science (Mathematics)

Programme :	<i>Master of Science (Mathematics)</i>	Year: V	Semester: X Paper: DSE Maths16C
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Subject: Mathematics

Course: DSE Maths16C	Course Title: Introduction to programming using MATLAB
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Course Outcomes: This course is useful to do mathematical computations using computer. It will help the students for better understanding of mathematical concepts.

Credits: 4	Discipline Specific Elective
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Max. Marks: As per Univ. rules	Min. Passing Marks: As per Univ. rules
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Unit	Content	Number of Hours
Unit I	MATLAB Basics: Introduction to MATLAB, Input and Output, Arithmetic, Algebra; Symbolic Expressions, Variables and Assignments, Solving Equations, Vectors and Matrices, Functions: Built-in Functions, User-Defined Functions.	12-15
Unit II	Data Classes: String Manipulation, Symbolic and Floating Point Numbers, Functions and Expressions, Complex Arithmetic, Matrices, Solving Linear Systems, Calculating	12-15

	Eigenvalues and Eigenvectors, Doing Calculus with MATLAB (Differentiation, Integration, Limits, Sums and Products, Taylor Series etc)	
Unit III	MATLAB Graphics: Two-Dimensional Plots, Parametric Plots, Contour Plots and Implicit Plots, Field Plots, Three-Dimensional Plots, Curves in Three-Dimensional Space, Surfaces in Three-Dimensional Space, Special Effects, Animations	13-15
Unit IV	MATLAB Programming: Branching with if, Logical Expressions, Branching with switch, Loops, User defined functions, M-Files	12-15
Note: Practical assignments using statistical and numerical techniques.		

Books Recommended:

Brian R. Hunt, Ronald L. Lipsman, Jonathan M. Rosenberg: A Guide to MATLAB for Beginners and Experienced Users, Cambridge University Press, 2001

Stormy Attaway: MATLAB A Practical Introduction to Programming and Problem Solving, Elsevier, 2017

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Pattern of Examination Theory Papers

1. Theory

Each theory paper shall consist of two sections A and B.

Section A (Short answers type with reasoning): 45 marks, eight questions of nine marks each, any five have to be attempted.

Section B (Long answers type): 30 marks, two questions of fifteen marks each, and both questions are compulsory with internal choice.

2. Internal assessment

For each theory paper internal assessment shall be conducted periodically (in the form of class tests and/or assignments/ group discussion/ oral presentation/ overall performance) during the semester period. Total marks allotted to internal assessment shall be 25. The evaluated answer sheets/assignments have to be retained by the Professor In-Charge for the period of six months and can be shown to the students if students want to see the evaluated answer sheets. The marks obtained by the students shall be submitted to the Head of concerned department/ the Principal of the College for uploading onto the University examination portal.